

Qualifying examination master's course Aerospace

Basics of thermodynamics

Prof. Dr. Wen / Prof. Dr. Jocher

Example examination

Date of the exam	Garching, June 12, 2020
Room	MW 1250
Start of the exam	9:00 a.m.
Duration of the exam	60 minutes
Type of exam	written
Approved tools	Writing and drawing utensils, calculator, dictionary

Exam-ID: 1
Name, first Name: _____
Student number: _____

The test information includes **15 Pages** (including cover sheet). In addition, a formula collection is issued. Please check the completeness immediately after receiving the test information. Label this cover page with your last name, first name and your student number. Sign this cover sheet too. At the end of the test, all worksheets and the formula collection must be submitted.

All tasks are to be answered on the task sheets (not on the formula collection). Please use the front and back of the sheets. Calculation results must be entered in the fields provided and are only evaluated with **solution path**. If partial tasks cannot be solved, make reasonable assumptions for the missing values for further calculation.

Signature: _____

Achievable points _____

Task:	1	2	3	4	5	Sum
Points:	7	7	8	9	29	60
Achieved points:						

1. Definitions and terms

(a) When is a system in thermodynamic equilibrium?

[7]

[2]

Solution:

A system is in thermodynamic equilibrium if its state variables do not change.

(b) Define the term phase!

[2]

Solution:

A phase is an area of matter that can be delimited from the environment and has the same thermodynamic, physical and chemical properties.

(c) Characterize the following systems according to their properties:

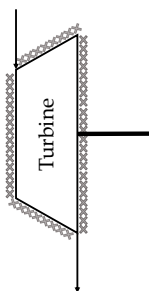
open – closed
diabat – adiabatic
static – dynamic

homogeneous - heterogeneous - continuous

If necessary, note the system limits shown!

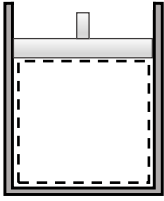
[3]

i. Fluid in a perfectly insulated turbine

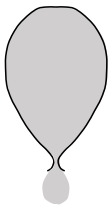




ii. Gas in a heat-permeable cylinder



iii. Air in the balloon with escaping gas



Solution:

- i. open/adiabatic/static/continuous
- ii. closed/diabatic/static/homogeneous
- iii. open/diabatic/static or dynamic/homogeneous



2. Thermal condition and ideal gas

(a) Name the three thermal state variables!!

[7]

[2]

Solution:

Pressure, temperature, specific or molar volume.

(b) Name the thermal equation of state of an ideal gas as a function of the universal gas constant R_m and the molar mass M .

[2]

Solution:

$$p \cdot v = \frac{R_m}{M} \cdot T$$

(c) In a container with the volume $V = 2 \text{ m}^3$ is the mass $m = 3 \text{ kg}$ of an ideal gas ($R_m = 8.314 \text{ J/molK}$). The pressure is $p = 1.5 \text{ bar}$, the temperature $T = 350 \text{ K}$

[3]

- i. What is the molar mass M and the amount of substance n of the gas.
- ii. The container is filled until its pressure is $p_2 = 2 \text{ bar}$. How big is the new mass of the gas in the container? Assume that the filling process is isothermal.

Solution:

i.

$$p \cdot V = m \cdot \frac{R_m}{M} \cdot T$$

$$M = m \cdot \frac{R_m}{p \cdot V} \cdot T = 29.1 \text{ kg/kmol}$$

$$n = \frac{m}{M} = 0.103 \text{ kmol}$$

ii.

$$m_2 = \frac{p_2 \cdot V \cdot M}{R_m \cdot T} = 4 \text{ kg}$$

3. First law of thermodynamics

- (a) Describe the statement of the 1st law of thermodynamics in your own words!

[8]

[2]

Solution:

The energy of a system can be changed in the form of heat, work, as well as the inflow and outflow of enthalpy, kinetic energy and potential energy.

- (b) Write down the 1st law of thermodynamics in general form as a power balance!

[2]

Solution:

$$\frac{dE_{sys}}{dt} = \sum_i \dot{Q}_i(t) + \sum_j \dot{W}_j(t) + \sum_e \dot{m}_e \left(h + \frac{c^2}{2} + gz \right)_e - \sum_i \dot{m}_i \left(h + \frac{c^2}{2} + gz \right)_i$$

- (c) In a steam boiler, $\dot{m} = 10^5 \text{ kg/h}$ water are evaporated every hour and the steam is expanded in a heat-insulated turbine. The specific enthalpy of the water at the boiler inlet is $h_1 = 128 \text{ kJ/kg}$, that of the steam at the boiler outlet and turbine inlet is $h_2 = 3150 \text{ kJ/kg}$ and at the turbine outlet $h_3 = 2350 \text{ kJ/kg}$.

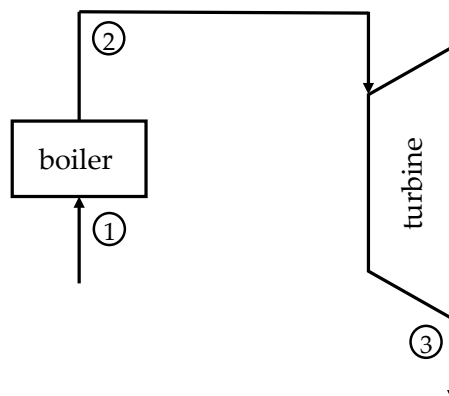


Abbildung 1: Sketch of the system

- i. How large is the heat flow supplied in the boiler \dot{Q}_K ?
- ii. What is the efficiency of the entire system?

[4]

Solution:

i. System boiler (operated stationary):

$$\frac{dE_{sys}}{dt} = \sum_i \dot{Q}_i(t) + \sum_j \dot{W}_j(t) + \sum_l \dot{m}_e \left(h_l + \frac{c_l^2}{2} + g \cdot z_l \right)$$

$$0 = \dot{Q}_K + \dot{m}(h_1 - h_2)$$

$$\dot{Q}_K = -\dot{m}(h_1 - h_2) = 83.9 \text{ MW}$$

ii. System turbine (operated stationary):

$$\frac{dE_{sys}}{dt} = \sum_i \dot{Q}_i(t) + \sum_j \dot{W}_j(t) + \sum_l \dot{m}_e \left(h_l + \frac{c_l^2}{2} + g \cdot z_l \right)$$

$$0 = \dot{W}_T + \dot{m}(h_2 - h_3)$$

$$\dot{W}_T = P_T = -22.2 \text{ MW}$$

This results in the efficiency:

$$\eta_{ges} = \frac{|P_T|}{\dot{Q}_K} = 0.265$$

4. Change of state and second law of thermodynamics

[9]

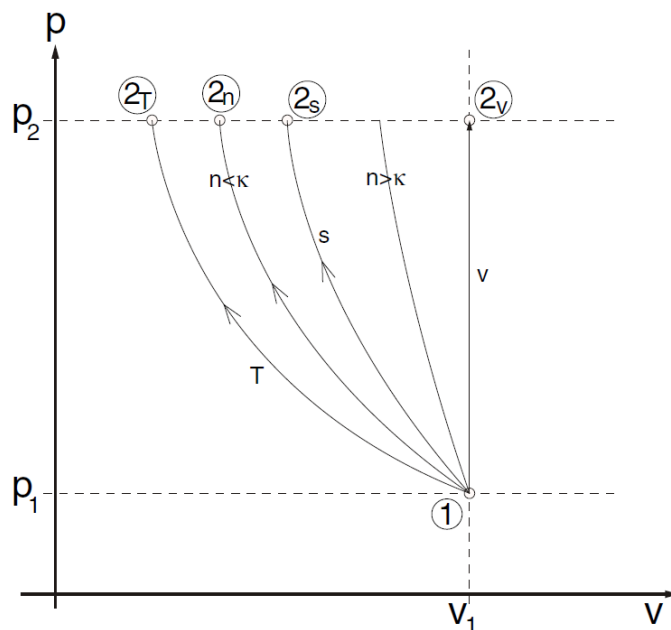
(a) Air compression: 10 kg air (ideal gas, $\kappa = 1.4$, $R_{Luft} = 287 \text{ J/kgK}$) are compressed from $T_1 = 293 \text{ K}$ and $p_1 = 0.95 \text{ bar}$ to $p_2 = 10 \text{ bar}$. This is supposed to happen

1. isochorously
2. isothermal
3. reversibly adiabatically and
4. polytropically with $n = 1.3$.

- i. Sketch the respective state change in the $p - v$ diagram!
- ii. Calculate the final temperature T_2 , the final volume V_2 and the transferred heat Q for the reversible adiabatic case!

[4]

Solution:



i.

ii.

$$\frac{p_2}{p_1} = \left(\frac{T_2}{T_1} \right)^{\frac{\kappa}{\kappa-1}}$$

$$T_2 = T_1 \cdot \left(\frac{p_2}{p_1} \right)^{\frac{\kappa-1}{\kappa}} = 572.33 \text{ K}$$



$$V_2 = \frac{m \cdot R \cdot T_2}{p_2} = 1.64 \text{ m}^3$$

For the heat $Q = 0$ applies because it is an adiabatic change of state..

- (b) Check whether the following statements about entropy are right or wrong. Incorrect answers result in point loss within the task. The minimum score within a task is 0.
- i. The entropy S is a state variable.
 - ii. The entropy S is a measure of the likelihood that a condition will occur.
 - iii. The entropy of a system can never decrease.
 - iv. Entropy can also be generated in reversible systems.
 - v. Systems can exchange entropy with the environment by transferring heat across the system boundary.

[5]

Solution:

- i. right
- ii. right
- iii. wrong
- iv. wrong
- v. right

5. Steam power plant

[29]

A large coal-fired power plant works in a simplified manner according to the following process:

- Saturated water in the feed water tank is at a pressure of $p_1 = 0.1 \text{ MPa}$ (state 1).
- The liquid water is brought to pressure $p_2 = 7 \text{ MPa}$ by the isentropic feed water pump (1 → 2).
- In the boiler, the water is preheated to the boiling line by the heat emitted when the coal is burned (2 → 3), completely evaporated (3 → 4) and superheated (4 → 5). A heat flow of $\dot{Q}_{th,2-5} = 1.3 \text{ GW}$ is transferred from the boiler to the working medium. While preheating and evaporation are isobaric, there is a pressure loss of $\Delta p_{4-5} = 0.5 \text{ MPa}$ while overheating.
- In the adiabatic high-pressure turbine (5 → 6) the water is expanded to a pressure of $p_6 = 1 \text{ MPa}$ polytropic. The isentropic efficiency of the high pressure turbine is $\eta_{is} = 0.8$
- In the isobaric reheater (6 → 7) the water is reheated up to temperature $T_7 = T_5$.
- In the adiabatic low-pressure turbine (7 → 8), the water is finally released up to pressure $p_8 = 5 \text{ kPa}$. There is wet steam in state 8. Losses result in an entropy flow of $\dot{S}_{irr,7-8} = 51 \frac{\text{kW}}{\text{K}}$ in the low-pressure turbine.
- The wet steam is fully condensed in the condenser (8 → 9). The heat generated is removed by cooling water, which is taken from the neighboring river.
- With the help of an auxiliary pump and the use of waste heat in the power plant, the water is finally brought back to the state of the tank (state 1).

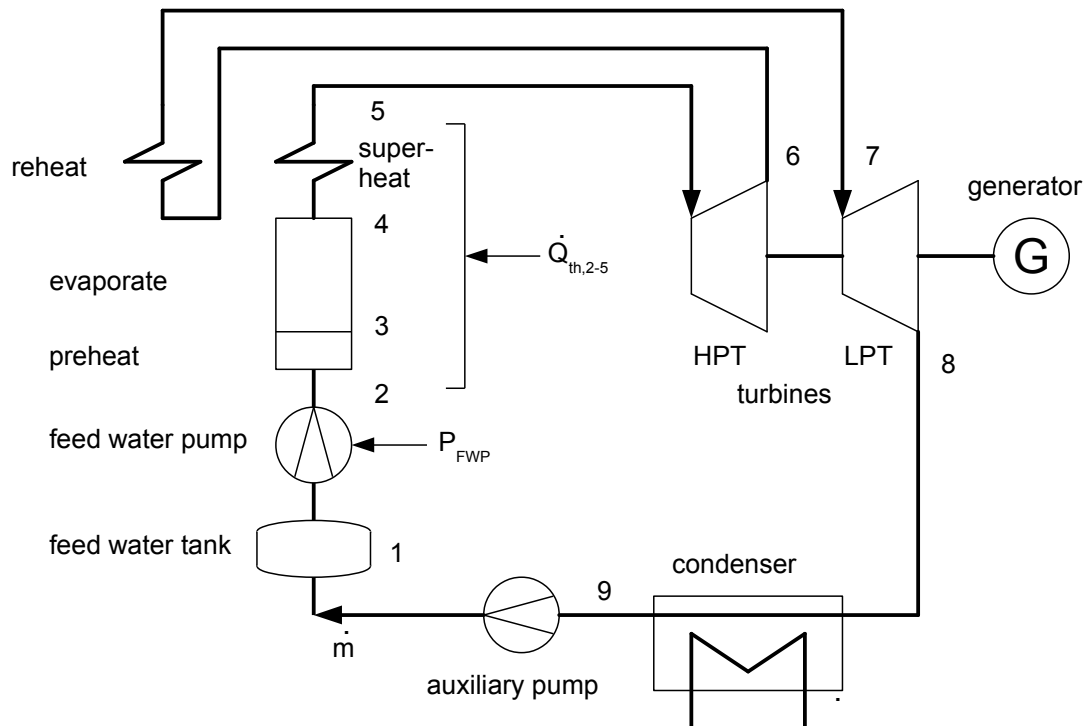


Abbildung 2: Sketch of the power plant process

Given Values:

Mass flow of the process: $\dot{m} = 420 \text{ kg/s}$

Storage: $p_1 = 0.1 \text{ MPa}$, $v_1 = 0,001 \text{ m}^3/\text{kg}$

Feed water pump: $p_2 = 7 \text{ MPa}$

Main boiler: $\dot{Q}_{th,2-5} = 1.3 \text{ GW}$, $\Delta p_{4-5} = 0.5 \text{ MPa}$

High pressure turbine: $p_6 = 1 \text{ MPa}$, $\eta_{is} = 0,8$, $\bar{c}_p|_5^6 = 1909.25 \frac{\text{J}}{\text{kg}\cdot\text{K}}$, $\kappa = 1.28$

Low pressure turbine: $p_8 = 5 \text{ kPa}$, $\dot{S}_{irr,7-8} = 51 \frac{\text{kW}}{\text{K}}$

Hints:

- All pressures are absolute pressures.
- Liquid water can be taken as an incompressible liquid, superheated steam as an ideal gas.
- Flow velocities and height differences can be neglected in all subtasks.
- If intermediate values from the steam tables are required, interpolate linearly between two neighboring values. Extrapolation of the values is not permitted.



Steam tables:

Saturation state:

p MPa	T °C	h' $\frac{\text{kJ}}{\text{kg}}$	h'' $\frac{\text{kJ}}{\text{kg}}$	s' $\frac{\text{kJ}}{\text{kg}\cdot\text{K}}$	s'' $\frac{\text{kJ}}{\text{kg}\cdot\text{K}}$
0.005	32.88	137.72	2560.5	0.476	8.393
0.1	99.63	417.51	2675.1	1.303	7.359
7	285.86	1267.9	2771.8	3.121	5.813

Superheated steam:

p MPa	T °C	h $\frac{\text{kJ}}{\text{kg}}$	s $\frac{\text{kJ}}{\text{kg}\cdot\text{K}}$
1	450	3370.8	7.6190
1	500	3478.3	7.7627
1	550	3587.1	7.8991
1	600	3697.4	8.0292
6.5	450	3296.3	6.680
6.5	500	3416.4	6.841
6.5	550	3534.6	6.989
6.5	600	3652.1	7.127
7	450	3289.1	6.637
7	500	3410.6	6.799
7	550	3529.6	6.948
7	600	3647.9	7.088

Tasks:

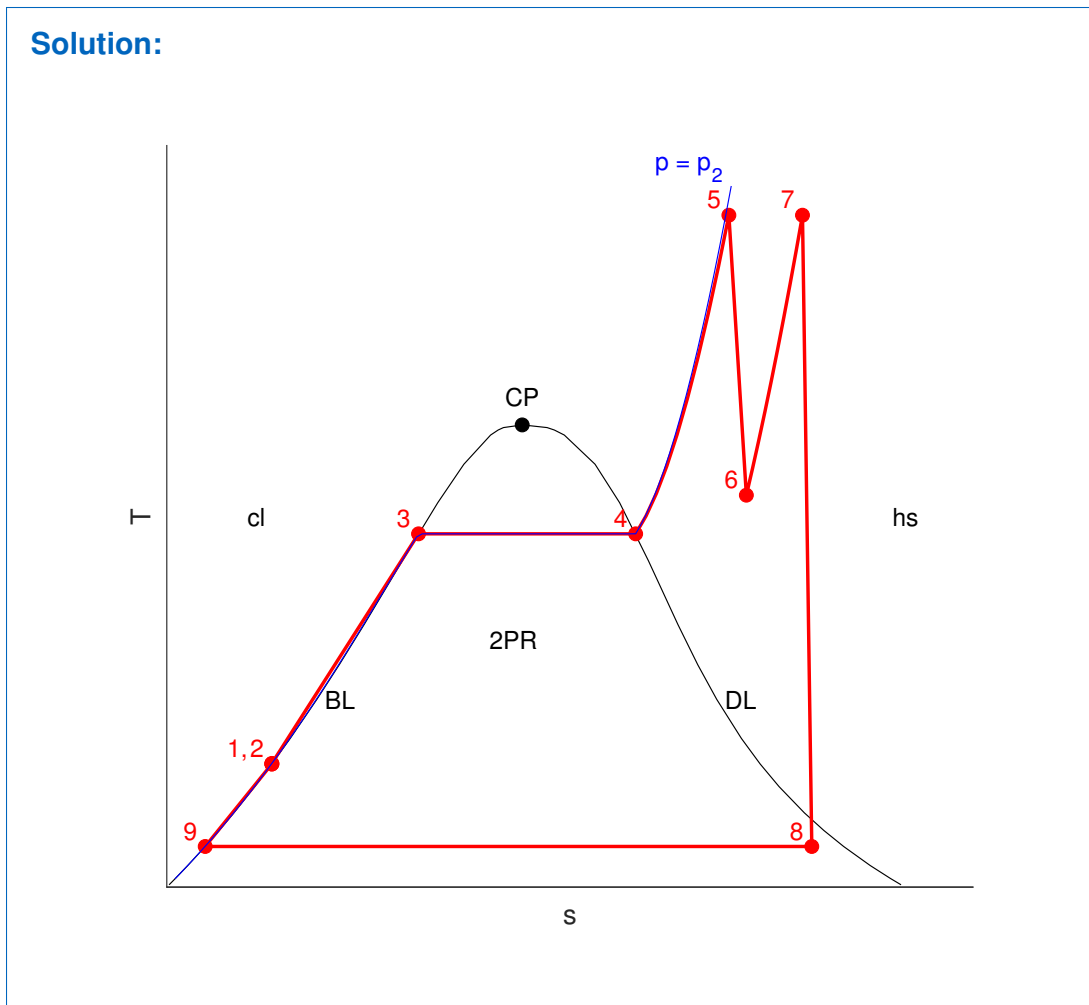
(a)

[10]

Qualitatively draw the T-s diagram of the power plant process. Draw in the following sizes and label them:

- Boiling line (BL), Dew line (DL) and critical point (CP). Label the areas „supercooled liquid “ (cl), „Two-phase region “ (2PR) and „superheated steam“ (hs).
- States 1-9 of the process as points.
- The state changes between the points. Pay attention to the characteristic course of the respective state change.
- The isobaric line for $p = p_2$. The line must go through all three areas (supercooled liquid, wet steam area, superheated steam).

Solution:



(b)

[2]

Determine the temperature T_1 and the specific enthalpy h_1 in the feed water tank.

Solution:

From the steam table for the state of saturation:

$$T_1 = 99.63^\circ\text{C}$$

$$h_1 = h' = 417.51 \frac{\text{kJ}}{\text{kg}}$$

(c)

[2]

Calculate the power delivered from the feed water pump to the working medium P_{FWP} . Also specify the temperature T_2 at the pump outlet.

Solution:

Compression work for an incompressible liquid:

$$\begin{aligned} P_{FWP} &= \dot{W}_{T,FWP} = \dot{m} \cdot w_{T,FWP} = \\ &= \dot{m} \cdot v_1 \cdot (p_2 - p_1) = 2.898 \text{ MW} \\ T_2 &= T_1 = 99.63^\circ\text{C} \end{aligned}$$

(d)

[5]

Calculate the temperature T_5 at the inlet of the high pressure turbine.

Solution:

First law of thermodynamics (power balance):

$$\frac{dE_{sys}}{dt} = \dot{m}_2 \cdot h_2 - \dot{m}_5 \cdot h_5 + \dot{Q}_{th,2-5} = 0$$

With:

$$\dot{m}_2 = \dot{m}_5 = \dot{m}$$

$$h_2 = h_1 + v_1 \cdot (p_2 - p_1) = 424.41 \frac{\text{kJ}}{\text{kg}}$$

For: h_5 :

$$h_5 = h_2 + \frac{\dot{Q}_{th,2-5}}{\dot{m}} = 3519.65 \frac{\text{kJ}}{\text{kg}}$$

Calculation of the pressure p_5 :

$$p_5 = p_2 - \Delta p_{4-5} = 6.5 \text{ MPa}$$

Using the steam table results from linear interpolation:

$$T_5 = 543.68^\circ\text{C} = 816.83\text{ K}$$

(e)

[5]

Calculate the temperature T_6 at the outlet of the high pressure turbine and the amount of power $|P_{HPT}|$ delivered by the high pressure turbine.

Solution:

Definition of the isentropic efficiency of a turbine with ideal gas as the working medium:

$$\eta_{is,T} = \frac{|w_t|}{|w_{t,is}|} = \frac{h_a - h_e}{h_{a,is} - h_e} = \frac{T_a - T_e}{T_{a,is} - T_e}$$

With $T_e = T_5$ and $T_a = T_6$.

Isentropic change of state:

$$\frac{T_{6,is}}{T_5} = \left(\frac{p_6}{p_5}\right)^{\frac{\kappa-1}{\kappa}}$$
$$T_{6,is} = T_5 \cdot \left(\frac{p_6}{p_5}\right)^{\frac{\kappa-1}{\kappa}} = 542.38\text{ K}$$

It results in:

$$T_6 = T_5 + \eta_{is,T} \cdot (T_{6,is} - T_5) = 597.27\text{ K}$$
$$|P_{HPT}| = |\dot{m} \cdot \bar{c}_p|_5^6 \cdot (T_6 - T_5) = 176.06\text{ MW}$$



(f)

[5]

How big is the steam content x_8 (respectively the wetness $(1 - x_8)$) at the outlet of the low pressure turbine? Why is excessive wetness in the low pressure turbine problematic?

Solution:

State variables at the inlet of the turbine:

$$T_7 = T_5 = 816.83 \text{ K}$$

$$p_7 = p_6 = 1 \text{ MPa}$$

$$s_7 = 7.8819 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$$

Second law of thermodynamics (entropy balance):

$$\frac{dS_{sys}}{dt} = \dot{m}_7 \cdot s_7 - \dot{m}_8 \cdot s_8 + \dot{S}_{irr,7-8} = 0$$

With:

$$\dot{m}_7 = \dot{m}_8 = \dot{m}$$

Finally, for s_8 :

$$s_8 = s_7 + \frac{\dot{S}_{irr,7-8}}{\dot{m}} = 8.0033 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$$

For each state variable z in the 2-phase region:

$$z = (1 - x) \cdot z' + x \cdot z'' = z' + x(z'' - z')$$

This results in the steam content respectively the wetness::

$$x_8 = \frac{s_8 - s'}{s'' - s'} = 0.95$$

$$(1 - x_8) = 0.05$$

The values for s' and s'' are taken from the steam table for $p = p_8$.

Excessive wetness in the low-pressure turbine leads to erosion of the turbine blades and must therefore be avoided.