Chair for Computer Aided Medical Procedures (CAMP) Master Seminar on Graph Deep Learning for Medical Applications SoSe22



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Basic Info about the course

- **Type**: Master Seminar (IN0014, IN2107, IN4431)
- Language: English
- **SWS**: 2
- ECTS: 5 Credits
- Webpage: https://wiki.tum.de/display/gdlma/GDLMA+SoSe22
- Time:
 - Tuesdays 12 pm to 2 pm
- Location:
 - Virtual Meeting Room (Zoom)
 - Seminar Room (03.09.012)
- Requirements:
 - Background in Machine/Deep Learning

https://www.youtube.com/watch?v=liv9R6BjxHM

Objective

- Learn through reading, understanding, presenting, and discussing
- Challenges in Medical Applications with Graph Deep Learning:
 - Current state of the art
 - Node classification, graph classification, graph learning, population level data analysis
 - Future challenges
 - 3D data, local and global data analysis in data distribution, learning with incomplete data
 - Handling Multi-Modal Data
 - Robustness and interpretability for GCN
 - Application to Medical imaging
 - Understanding the mathematical details

Course Evaluation

Presentation (45%)

- 20 minutes + 10 minutes Q&A
- Slides (Powerpoint, Latex, see website for templates)
- They should cover all relevant aspects of the paper
 - Motivation
 - Methodology
 - Experimental results
 - Take Home Message
 - Discussion

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- Self-contained (review of state of the art is necessary!)
- Presentation guidelines will be released later.
- All students are expected to attend all presentations and interact during Q&A
- Examples from previous semester:

https://wiki.tum.de/display/dlma/Presentations%3A+Summer+202

Blog Post (45%)

- Blog post explaining the main ideas of the paper.
 - Motivation + Contributions
 - Methodology
 - Results & Discussion
- You can refer to https://bair.berkeley.edu/blog/ to get ideas
- 1500-1700 words paper summary + 200-300 words your own review
- Students will be requested to comment on each other's blog posts.
- The website where the posts will be uploaded is [1].
- You can later privately share your blog posts in other websites as well (eg Medium).
- Upload the blog post two weeks before presentation. There will be discussion until presentation
- Examples from previous semester:

https://wiki.tum.de/display/dlma/Blog%3A+Summer+2020

Attendance and Participation (10%)

Schedule

Sessions will take place **Tuesdays from 12:00 to 14:00h**. A group of Two to Three students will present their papers during each session.

Date	Time	Place	Торіс
26 04 22	12.00 - 14.00	03 09 012	Lecture: Intro to GDI MA
03.05.22	12:00 - 14:00	03.09.012	Paper session
10.05.22	12:00 - 14:00	03.09.012	Paper session
17.05.22	12:00 - 14:00	03.09.012	Talk 1: Dr. Seyed Ahmad Ahmadi (NVIDIA)
24.05.22	12:00 - 14:00	03.09.012	Paper session
31.05.22	12:00 - 14:00	03.09.012	Paper session
14.06.22	12:00 - 14:00	03.09.012	Talk 2 : Alaa Bessadok (Helmholtz)
21.06.22	12:00 - 14:00	03.09.012	Paper session
28.06.22	12:00 - 14:00	03.09.012	Lecture: Intro to Scene Graphs
5.07.22	12:00 - 14:00	03.09.012	Paper session
12.07.22	12:00 - 14:00	03.09.012	Paper session
19.07.22	12:00 - 14:00	03.09.012	Talk 3 : Azade Farshad (CAMP)
26.07.22	12:00 - 14:00	03.09.012	Paper session - Backup

Paper assignments: https://wiki.tum.de/display/gdlma/GDLMA+SoSe22



Graph Deep Learning for Medical Applications

Lecture I



26.04.2022

Geometric Deep Learning (GDL)

"Geometric deep learning is an umbrella term for emerging techniques attempting to generalize (structured) deep neural models to non-Euclidean domains, such as graphs and manifolds."

Non-Euclidean Spaces





Point Clouds



Graphs

[1] https://www.researchgate.net/figure/Remeshing-the-Stanford-Bunny-Left-Pure-quad-remeshing-Right-detail-of-a-half-pole_fiq9_221316594

[2] Yang, Guandao, et al. "Pointflow: 3d point cloud generation with continuous normalizing flows." (2019).

[3] https://commons.wikimedia.org/wiki/File:Social_Network_Analysis_Visualization.png

G = (V, E)

• Set of nodes (arbitrary ordering) and edges



G = (V, E)

- Set of nodes (arbitrary ordering) and edges
- Feature vector for each node



G = (V, E)

- Set of nodes (arbitrary ordering) and edges
- Feature vector for each node
- Edge attributes





Convolutional Networks



Images vs. Graphs



Images

- well-structured, grid-based
- Fixed number of neighbours
- Fixed position

\rightarrow Convolution using Filters



Graphs

- Flexible data structure
- Varying number of neighbours
- Flexible position of nodes
- → Graph Convolution

Graph Neural Networks

Learning directly on graph-structured data

Graph Neural Network Tasks

Node Classification/Regression

Determine a label for each node.



Input graph: unlabeled or partially labeled nodes



Output graph: labeled nodes

Graph Neural Network Tasks

Graph Classification/Regression

Classify the whole graph into different categories.



Input: set of graphs

Output: labels for each graph, (e.g., "does the graph contain two rings?")

Graph Neural Network Tasks

Link Prediction

Predict whether an edge exists between two given nodes or not.



Input: Incomplete graph

Output: Graph with predicted edges

Transduction:

→ Reasoning from observed, specific (training) cases to specific (test) cases

- All data is observed beforehand (training and testing)
- Labels of the test data is unknown
- But the test data points are used during the learning process
- \rightarrow Does not work for new/unseen data

Induction:

 \rightarrow Reasoning from observed (training) data to general rules, which are then applied to test cases

- Equivalent to supervised learning
- Only training data is used during learning
- Then the learned rules are applied to new unseen (test) data

\rightarrow Also works for new/unseen data



Example from [Belkin et al., JMLR 2006]



Example from [Belkin et al., JMLR 2006]





Spectral vs. Spatial GNNs

Spectral

- The method works in the **eigenvalue domain** of the feature representation
- The eigenvalue domain is defined by the **complete dataset** (a local structure in the graph affects the global representation)

 \rightarrow Extension to unseed data not easily possible

 \rightarrow Transductive Learning

Spatial

- Using the node neighbourhood
- Instead of the eigenvalue domain

 \rightarrow An extension to new samples is possible without retraining the network

 \rightarrow Inductive (and Transductive) Learning

Spectral vs. Spatial GNNs



Graph



Adjacency Matrix

	Α	\mathbf{B}	\mathbf{C}	D	\mathbf{E}	\mathbf{F}	G
Α	٢0	1	0	0	0	0	ך 0
В	1	0	1	0	0	0	0
\mathbf{C}	0	1	0	1	1	1	1
D	0	0	1	0	0	0	0
\mathbf{E}	0	0	1	0	0	0	0
\mathbf{F}	0	0	1	0	0	0	0
\mathbf{G}	0	0	1	0	0	0	0

Graph



$$D_v = \sum_u A_{vu}.$$

The degree of node v is the number of edges incident at v.

Degree Matrix



Laplacian

$$L =$$
 Laplacian of the Graph
 $D =$ Degree Matrix of the Graph
 $A =$ Adjacency Matrix of the Graph



- Laplacian is a **real**, **symmetric** matrix, which means it has all real eigenvalues
- The set of eigenvalues of the Laplacian is called its 'spectrum'
- \rightarrow Spectral Graph Convolutions

Polynomials of the Laplacian :

$$p_w(L) = w_0 I_n + w_1 L + w_2 L^2 + \ldots + w_d L^d = \sum_{i=0}^d w_i L^i.$$

These polynomials can be thought of as the equivalent of 'filters' in CNNs, and the coefficients was the weights of the 'filters'.

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Resulting convolution:

$$x'=p_w(L)\;x$$

$$p_w(L)=w_0I_n+w_1L+w_2L^2+\ldots+w_dL^d=\sum_{i=0}^d w_iL^i.$$

$$x'=p_w(L)\;x=\sum_{i=0}^d w_iL^ix=w_0I_nx=x.$$

$$p_w(L)=w_0I_n+w_1L+w_2L^2+\ldots+w_dL^d=\sum_{i=0}^dw_iL^i.$$

$$egin{aligned} x_v' &= (Lx)_v = L_v x \ &= \sum_{u \in G} L_{vu} x_u \ &= \sum_{u \in G} (D_{vu} - A_{vu}) x_u \ &= D_v \; x_v - \sum_{u \in \mathcal{N}(v)} x_u \end{aligned}$$

$$p_w(L)=w_0I_n+w_1L+w_2L^2+\ldots+w_dL^d=\sum_{i=0}^dw_iL^i.$$



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Spectral vs. Spatial GNNs


General idea of inductive graph approach

General idea for spatial GCN:

Feature representation of one node gets updated by surrounding nodes



Node 1 with feature representation v₁ has connections to five corresponding neighbors

General idea of inductive graph approach

General idea for spatial GCN:

Feature representation of one node gets updated by surrounding nodes



Node 1 with feature representation v₁ has connections to five corresponding neighbors Surrounding nodes features are aggregated and result in new representation v'₁

Spatial GCN:

$$egin{aligned} egin{aligned} h_v^{(k)} &=& f^{(k)} \left(egin{aligned} && \sum\limits_{u \in \mathcal{N}(v)} h_u^{(k-1)} \ && V \end{aligned}
ight) & ext{for all } v \in V. \end{aligned}$$



https://distill.pub/2021/understanding-gnns/

Kipf, Welling. "Semi-Supervised Classification with Graph Convolutional Networks", 2016.



$$W^{(1)} = 1, B^{(1)} = 1$$

$$\begin{aligned} h_A^{(1)} &= f(W^{(1)} \times \frac{h_C^{(0)} + h_E^{(0)}}{2} + B^{(1)} \times h_A^{(0)}) \\ &= f(1 \times \frac{-10 + 3}{2} + 1 \times 6) \\ &= f(-3.5 + 6) \\ &= f(2.5) \\ &= ReLU(2.5) = 2.5 \end{aligned}$$

Practical example on spatial GCN:



$$egin{aligned} h_v^{(k)} &= f^{(k)} \left(W^{(k)} \cdot rac{\sum\limits_{u \in \mathcal{N}(v)} h_u^{(k-1)}}{|\mathcal{N}(v)|} + B^{(k)} \cdot egin{matrix} h_v^{(k-1)} \ dots \end{pmatrix} \end{aligned}
ight) \end{aligned}$$

$$h_{E}^{(1)} =$$

 $W^{(1)} = 1, B^{(1)} = 1$



$$egin{aligned} h_v^{(k)} &= f^{(k)} \left(W^{(k)} \cdot rac{\sum\limits_{u \in \mathcal{N}(v)} h_u^{(k-1)}}{|\mathcal{N}(v)|} + B^{(k)} \cdot egin{aligned} h_v^{(k-1)} \ |\mathcal{N}(v)| \end{array}
ight) \end{aligned}$$

$$h_E^{(1)} = f(W^{(1)} \times \frac{h_A^{(0)} + h_B^{(0)} + h_D^{(0)}}{3} + B^{(1)} \times h_E^{(0)})$$

$$W^{(1)} = 1, B^{(1)} = 1$$



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ight) \end{aligned}$$

$$\begin{aligned} h_E^{(1)} &= f(W^{(1)} \times \frac{h_A^{(0)} + h_B^{(0)} + h_D^{(0)}}{3} + B^{(1)} \times h_E^{(0)}) \\ &= f(1 \times \frac{6+2+1}{3} + 1 \times 3) \end{aligned}$$



$$W^{(1)} = 1, B^{(1)} = 1$$

$$h_A^{(1)} = f(W^{(1)} \times \frac{h_C^{(0)} + h_E^{(0)}}{2} + B^{(1)} \times h_A^{(0)})$$

= $f(1 \times \frac{-10 + 3}{2} + 1 \times 6)$
= $f(-3.5 + 6)$
= $f(2.5)$
= $ReLU(2.5) = 2.5$
$$h_E^{(1)} = f(W^{(1)} \times \frac{h_A^{(0)} + h_B^{(0)} + h_D^{(0)}}{3} + B^{(1)} \times h_E^{(0)})$$

= $f(1 \times \frac{6 + 2 + 1}{3} + 1 \times 3)$
= $f(3 + 3)$

$$= f(6)$$
$$= ReLU(6) = 6$$

Practical example on spatial GCN:



Iteration 0

Iteration 1

Example 1: GraphSage

General idea:

Feature representation of one node gets updated by surrounding nodes



Example 2: Graph Attention Network (GAT)

General idea:

Network learns which neighbors are the most important for the update (attention



[1] P. Veličković, G. Cucurull, A. Casanova, A. Romero, P. Lio and Y. Bengio, 2017. Graph attention networks ICLR 2018

Applications of GDL in Medicine





Population Graph



- Each subject is represented as one node in the graph
- Sharing information across whole patient population
- Combining multi-modal information, e.g. clinical data, imaging data, genetics,...



Population Graph - an Example



- Integration of clinical data and image data
- Subjects can be connected based on similarity e.g.



Population Graph - an Example





image information can be stored in node features

- Integration of clinical data and image data
- Subjects can be connected based on similarity e.g.



Population Graph - an Example



- Usage of Graph Neural Networks (GNNs) to learn patient specific predictions
 - Idea: allow **information propagation** among neighbourhoods to learn from similar subjects



MedGCN: Medical Graph Convolutional Network





- Connecting Patients, Encounters, Lab results and Medication
- Tasks:
 - Medication recommendation
 - Lab test imputation

Disease Detection using Brain Connectivity Networks





- Detection of Discriminative Neurological Circuits
- Usage of fMRI Sequences
- Applications: Alzheimer's Disease, Obsessive-Compulsive Disorder, Parkinson's Disease, Autism Spectrum Disorder, etc.

Fig.: Xing, et al. "Detection of Discriminative Neurological Circuits Using Hierarchical Graph Convolutional Networks in fMRI Sequences.", 2020., Li, et al. "Graph neural network for interpreting task-fmri biomarkers.", 2019., Ma, et al. "Deep graph similarity learning for brain data analysis.", 2019.

Comorbidity Detection





- Using matrix completion to predict unknown comorbidities
- Recovering missing links in the bipartite graph for health risk predictions

Histopathological Image Classification for Breast Cancer Subtyping





- (a) **Cell Graph:** cells and cellular interactions
- (b) **Tissue Graph:** region adjacency graph
- (c) HierArchical-Cell-to-Tissue (HACT) representation: combination of (a) and (b)

Drug Discovery





- Using Graph Convolutional Networks to predict drug properties
- Capturing subtle substructure patterns



Geometric Deep Learning

- allows to perform learning on datasets in non-Euclidean spaces
- operates on graphs, meshes, point clouds,...

Graph Neural Networks

- operate on graph-structured data specifically
- are used to solve three main tasks: node classification, graph classification, link prediction
- operate on spectral or spatial domain

Recap:



When?

- Intrinsic non-Euclidean structure of the dataset: molecules, social networks, meshes...
- Multimodal applications

How?

- Define **graph structure** if necessary: population graph, connectivity graph, region adjacency graph...
- Specify **node features** and **edges** (and potentially edge weights)
- Define the **type of problem**: node classification, graph classification, edge prediction
- Choose a graph learning algorithm
- Train the network :D

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Pros and Cons

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Pros

- Allows utilisation of complex inter-connected data
- Multimodal applications
- Expansion of Deep Learning to new fields \rightarrow novel research
- Performance gain in some applications (e.g. social networks, molecule predictions)

Cons

- Sometimes the graph structure is not defined/unique
- Highly dependent on underlying structure of the data
- Fairly new \rightarrow fewer content (tutorials, examples..) than other types of models.

Setting:

- We have clinical data
- and image data of 1000 patients

Goal:

• We want to predict the estimated time of survival for each patient

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Node Classification







Graph Classification

Setting:

- We have clinical data
- and image data of 1000 patients

Goal:

• We want to predict the estimated time of survival for each patient







Graph Classification

Patient Population Graph



Setting:

- We have fMRI data of brain scans of 100 patients
- We don't know any relationships between patients

Goal:

• We want to decide whether a patient has Alzheimer's Disease

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Node Classification





Graph Classification

Edge Prediction

Setting:

- We have fMRI data of brain scans of 100 patients
- We don't know any relationships between the patients

Goal:

• We want to decide whether a patient has Alzheimer's Disease









Edge Prediction

One Individual Graph per Patient





Advancements in the field of inductive graph learning



[2] P. Veličković, G. Cucurull, A. Casanova, A. Romero, P. Lio and Y. Bengio, 2017. Graph attention networks ICLR 2018

[3] Liyu Gong, Qiang Cheng, Exploiting Edge Features in Graph Neural Networks, CVPR 2019

[4] Ying, C., Cai, T., Luo, S., Zheng, S., Ke, G., He, D., ... & Liu, T. Y. (2021). Do Transformers Really Perform Badly for Graph Representation?. Advances in Neural Information Processing Systems, 34. v_4

Advancements in the field of inductive graph learning







H. Burwinkel, A. Kazi, G. Vivar, S. Albarqouni, G. Zahnd, N. Navab, S. A. Ahmadi, Adaptive Image-Feature Learning for Disease Classification Using Inductive Graph Networks, MICCAI 2019
 H. Burwinkel, M. Keicher, D. Bani-Harouni, T. Zellner, F. Eyer, N. Navab, S. A. Ahmadi, Decision Support for Intoxication Prediction Using Graph Convolutional Networks, MICCAI 2020
 Keicher, M., Burwinkel, H., Bani-Harouni, D., Paschali, M., Czempiel, T., Burian, E., ... & Wendler, T. (2021). U-GAT: Multimodal Graph Attention Network for COVID-19 Outcome Prediction. 71 arXiv preprint arXiv:2108.00860.

U-GAT: Multimodal Graph Attention Network for COVID-19 Outcome Prediction



Keicher, M., Burwinkel, H., Bani-Harouni, D., Paschali, M., Czempiel, T., Burian, E., ... & Wendler, T. (2021). U-GAT: Multimodal Graph Attention Network for COVID-19 Outcome Prediction. arXiv preprint arXiv:2108.00860.
KNN Graph Construction with Mutual Information Weighted Features



Keicher, M., Burwinkel, H., Bani-Harouni, D., Paschali, M., Czempiel, T., Burian, E., ... & Wendler, T. (2021). U-GAT: Multimodal Graph Attention Network for COVID-19 Outcome Prediction. arXiv preprint arXiv:2108.00860.

Results ICU Prediction

Task	Architecture	AP	DICE
Segmentation	U-Net	-	$\textbf{64.14} \pm \textbf{1.76}$
ICU	MLP	57.65 ± 10.84	_
ICU	ResNet18	66.97 ± 9.68	_
ICU	U-Net*+KNN	61.17 ± 9.94	(64.14 ± 1.76)
ICU	U-Net*+MLP	61.50 ± 12.69	(64.14 ± 1.76)
ICU	U-Net*+GCN	68.75 ± 15.07	(64.14 ± 1.76)
ICU	ResNet18-GAT	63.70 ± 16.52	_
ICU	U-Net*+GAT	69.80 ± 12.04	(64.14 ± 1.76)
ICU+Seg.	U-Net-GAT	$\textbf{69.94} \pm \textbf{14.85}$	61.39 ± 2.16
Multilabel+Seg.	U-Net-GAT	64.89 ± 12.82	60.70 ± 1.85

* end-to-end training



Fig. 5. Left: Batch graph showing the attention scores of a single test patient. The thickness of the line corresponds to the attention score of the respective neighbors after two hops. Right: CT images, segmentation ground truth and predicted segmentation of a single axial and coronal slice from the test patient and the neighbor with maximum attention. Bottom: Most important features for the test patient and the neighbor with maximum attention. In brackets, the radiomics predicted by the pretrained U-Net are shown.

Keicher, M., Burwinkel, H., Bani-Harouni, D., Paschali, M., Czempiel, T., Burian, E., ... & Wendler, T. (2021). U-GAT: Multimodal Graph Attention Network for COVID-19 Outcome Prediction. arXiv preprint arXiv:2108.00860.



Differentiable graph module (DGM) for graph convolutional networks.



Benchmark datasets: CiteSeer, PubMed, Cora. Medical Datasets: Tadpole, UK Biobank. Computer Vision Datasets: Shapenet, Animals with Attribute 2 dataset

Kazi, A., Cosmo, L., Navab, N. and Bronstein, M., 2020. Differentiable graph module (dgm) for graph convolutional networks. *arXiv* preprint arXiv:2002.04999. Accepted in PAMI 2022.

Graph-in-graph



Main idea is to obtain the population graph on graph-based data by learning the graph structure and ensuring normal nodes degree distribution.

Mullakaeva, K., Cosmo, L., Kazi, A., Ahmadi, S. A., Navab, N., & Bronstein, M. M. (2022). Graph-in-Graph (GiG): Learning interpretable latent graphs in non-Euclidean domain for biological and healthcare applications. *arXiv preprint arXiv:2204.00323*.

Time for Questions